#### Shape & Space

**Circles** 

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The parts of a circle



centre - the point within the circle where the distance to points on the circumference is the same.

radius - the distance from the centre to any point on the circle. The diameter is twice the radius.

circumference(perimeter) - the distance around a circle.

**chord** is a straight line joining two points on the circumference.

diameter - a chord (of max. length) passing through the centre

sector - a region enclosed by two radii and an arc.

segment - the region enclosed by a chord and an arc of the circle.

tangent - a straight line making contact at one point on the circumference, such that the radius from the centre is at right angles to the line.

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### Subtended angles

When a chord subtends an angle on the circumference of a circle, the angle subtended at the centre of the circle is twice the angle.



A diameter subtends a right-angle at the circumference



angle XPZ = 90 deg.

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Angles subtended by a chord onto the circumference of a circle are equal.





Chords



The line joining the centre of a circle and the mid-point of a chord is perpendicular to the chord. The chord is bisected into two equal halves.

XP = PY

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## **Tangents**



The tangents to a circle from a point are equal in length.

AP = BP

also,

the tangents subtend equal angles at the centre of the circle

# angle POA = angle POB

and,

the angles between the tangents and the line joining the centre of the circle and the point are equal.

angle APO = angle BPO

**note** : Triangle APO and triangle BPO are congruent.

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### The angle between a tangent and a chord

The angle between a tangent and a chord is equal to the angle subtended by the chord in the opposite segment.



angle ZPY = angle PXY

Cyclic quadrilaterals

Opposite angles in a cyclic quadrilateral add up to 180 deg.



As with all quadrilaterals, the **sum of the interior angles = 360 deg**.

Any exterior angle of a cyclic quadrilateral equals the interior opposite angle.